



**Q1**

a) Express  $\frac{2\pi}{5}$  radians in degrees.

$$2\pi \text{ rads} = 360^\circ \dots \text{ divide both sides by } 5$$

$$\frac{2\pi}{5} \text{ rads} = \frac{360^\circ}{5} = 72^\circ$$

b) Express  $210^\circ$  in radians.

$$360^\circ = 2\pi \text{ rads} \dots \text{ divide both sides by } 360$$

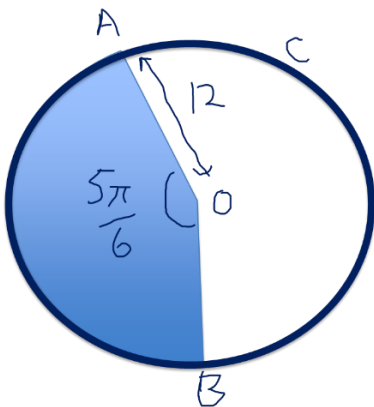
$$1^\circ = \frac{2\pi}{360} \text{ rads} = \frac{\pi}{180} \text{ rads} \dots \text{ multiply both sides by } 210$$

$$210^\circ = \frac{210\pi}{180} \text{ rads} = \frac{7\pi}{6} \text{ rads} \approx 3.67 \text{ rads}$$

**Q2**

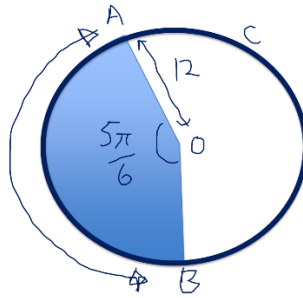
The diagram shows a circle  $c$  with centre  $O$  and radius  $12\text{cm}$ . Also shown is the minor sector  $ABO$ . The minor arc  $[AB]$  subtends an angle of  $\frac{5\pi}{6}$  rads at the centre.

i (i) Label the diagram.



ii (ii) Find the length of the minor arc [AB]

$$\begin{aligned}
 l &= r\theta \\
 &= 12 \times \frac{5\pi}{6} \\
 &= 10\pi \text{ cm}
 \end{aligned}$$



(ii) Find the area of the major sector ABO

$$\begin{aligned}
 A &= \frac{1}{2}r^2\theta \\
 \theta &= 2\pi - \frac{5\pi}{6} = \frac{7\pi}{6} \\
 A &= \frac{1}{2} \times 12^2 \times \frac{7\pi}{6} = 84\pi \text{ cm}^2
 \end{aligned}$$

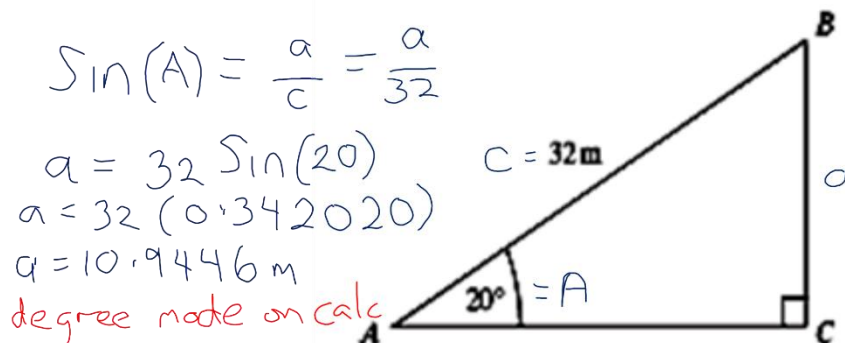
### Q3

The diagram shows a triangle ABC.

Angle A = 20° and angle C = 90° AB = 32m

Calculate the height |BC|.

Solve the triangle.



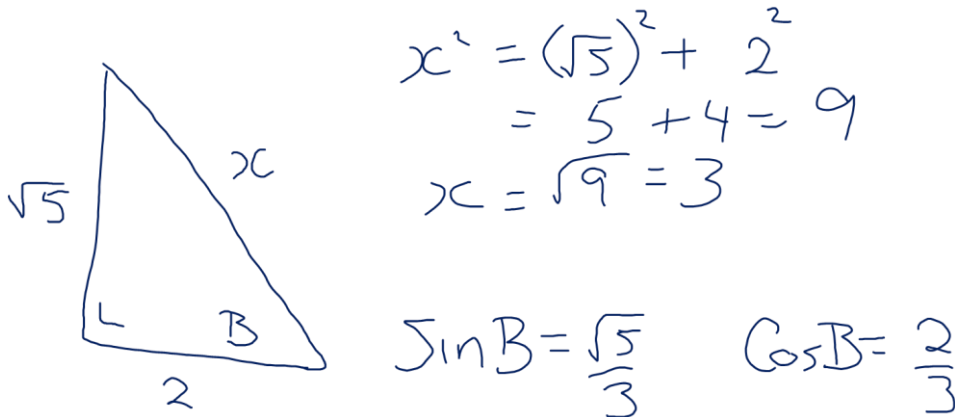
You can then solve for |AC| using the Pythagoras Theorem.

And the sum of the three angles in a triangle = 180, so:

$$\angle ABC = 180 - 90 - 20 = 70 \text{ degrees}$$

**Q4**

If  $\tan B = \sqrt{5}/2$ , find the value of  $\sin B$  and  $\cos B$ .

**Q5**

1) Find  $\cos 72^\circ 18'$ , correct to 4 decimal places.

Method 1

calculator:

$$\boxed{\cos} \ 72 \ \boxed{000} \ 18 \ \boxed{0000} \ \boxed{=}$$

$$= 0.30403306$$

$$= 0.3040 \text{ to 4 d.p.}$$

Method 2

$$72 + \frac{18}{60} = 72.3$$

$$\cos(72.3) = 0.30403306$$

$$= 0.3040 \text{ to 4 dp}$$

2) If  $\sin A = 0.5216$ , find  $A$  correct to the nearest second.

Method 1

$$\sin^{-1}(\sin A) = \sin^{-1}(0.5216)$$

$$A = \boxed{\text{Shift}} \boxed{\text{Sin}} 0.5216$$

$$= 31.43963765^\circ$$

$$\boxed{0.111} = 31^\circ 26' 22.7''$$

$$= 31^\circ 26' 23'' \text{ to nearest second}$$

**Method 2**

$$31.43963765^\circ$$

$$= 31^\circ + 0.43963765 \times 60'$$

$$= 31^\circ + 26.37825916'$$

$$= 31^\circ + 26' + 0.37825916 \times 60''$$

$$= 31^\circ 26' 22.6955'' = 31^\circ 26' 23'' \text{ to nearest sec}$$

3) If  $\sin A = 4/7$ , find A

$$\sin^{-1}(\sin A) = \sin^{-1}\left(\frac{4}{7}\right)$$

$$A = \boxed{\text{Shift}} \boxed{\text{Sin}} \boxed{4} \boxed{\div} \boxed{7} \boxed{)} \boxed{=} \checkmark$$

$$A = \boxed{\text{Shift}} \boxed{\text{Sin}} 4 \boxed{\div} 7 \boxed{=} \times$$

$$A = 34.8^\circ$$

4) Given  $D = 3/4\pi$  Rads find cosec D

Cosec is the reciprocal of Sine

$$\text{Cosec}\left(\frac{3\pi}{4}\right) = \left(\sin\left(\frac{3\pi}{4}\right)\right)^{-1} = \frac{1}{\sin\left(\frac{3\pi}{4}\right)}$$

Radian Mode = 1.414213562

$$\boxed{)} \boxed{\text{Sin}} \boxed{)} \boxed{3} \boxed{\pi} \boxed{\div} \boxed{4} \boxed{)} \boxed{)} \boxed{x^{-1}} \boxed{=} \checkmark$$

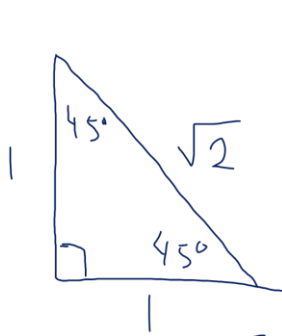
**Q6**

Make sketches of the following triangles:

- An Isosceles right-angled triangle with sides = 1 unit.

- An Equilateral triangle with sides = 2 units. Draw a line to divide this triangle into two equal right-angled triangles.

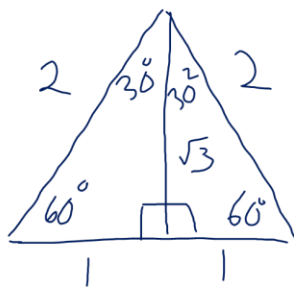
Solve all three triangles and hence calculate Sin, Cos and Tan of 30°, 45° and 60° in surd form.



Pythagoras  
 $x^2 = 1^2 + 1^2 = 2$   
 $x = \sqrt{2}$   
 $\theta + \theta + 90^\circ = 180^\circ$   
 $\theta = 45^\circ$

$$\sin 45^\circ = \frac{1}{\sqrt{2}} \quad \tan 45^\circ = \frac{1}{1} = 1$$

$$\cos 45^\circ = \frac{1}{\sqrt{2}}$$



$60^\circ - 2 = 30^\circ$   
 $y^2 + 1^2 = 2^2$   
 $y^2 = 4 - 1 = 3$   
 $y = \sqrt{3}$

$$\sin 60^\circ = \frac{\sqrt{3}}{2}$$

$$\tan 60^\circ = \frac{\sqrt{3}}{1} = \sqrt{3}$$

$$\sin 30^\circ = \frac{1}{2}$$

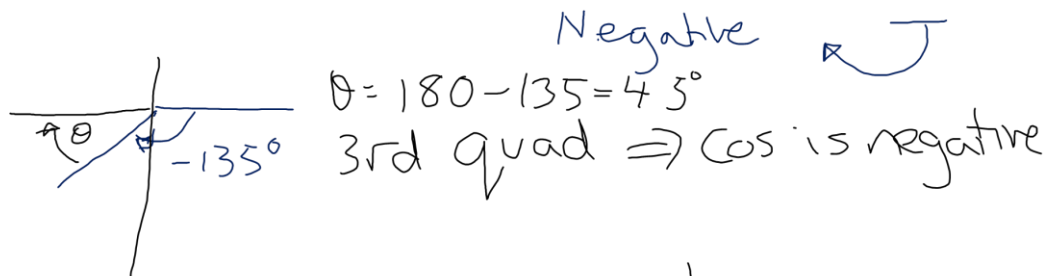
$$\cos 30^\circ = \frac{\sqrt{3}}{2}$$

$$\cos 60^\circ = \frac{1}{2}$$

$$\tan 30^\circ = \frac{1}{\sqrt{3}}$$

**Q7**

1) Express in surd form,  $\cos(-135^\circ)$ .

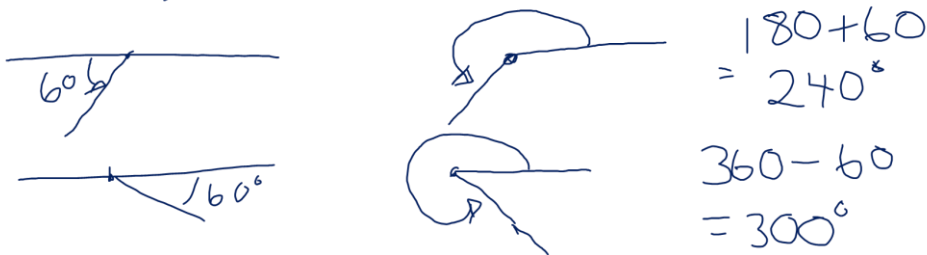


$$\cos(-135^\circ) = -\cos 45^\circ = -\frac{1}{\sqrt{2}}$$

check on calculator. but question asked for surd form.

2) If  $\sin x = -\sqrt{3}/2$ , find two values for  $x$  if  $0^\circ \leq x \leq 360^\circ$ .

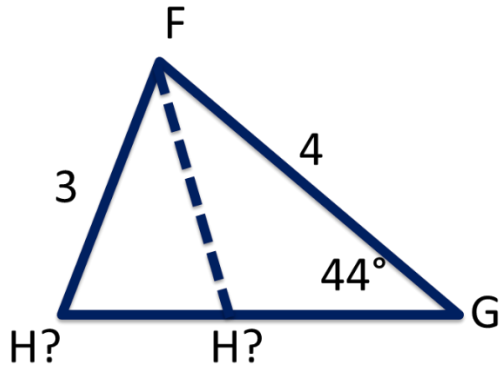
Answer is negative Sin is negative in 3rd + 4th Q  
 $\sin^{-1}\left(\frac{\sqrt{3}}{2}\right) = 60^\circ$  (pg 13 of formulae)



**Q8**

In a triangle  $FGH$ ,  $|FG| = 4\text{cm}$ ,  $|FH| = 3\text{cm}$  and  $|\angle FGH| = 44^\circ$ .

Find the possible values of  $\angle FHG$ .



Use the Sine Rule

Pair? Yes =  $G$  and  $g$ . Second Pair? Have  $h$  but looking for  $H$ .

$$\frac{\sin H}{h} = \frac{\sin G}{g}$$

$$\sin H = h \frac{\sin G}{g}$$

$$H = \sin^{-1}\left(h \frac{\sin G}{g}\right)$$

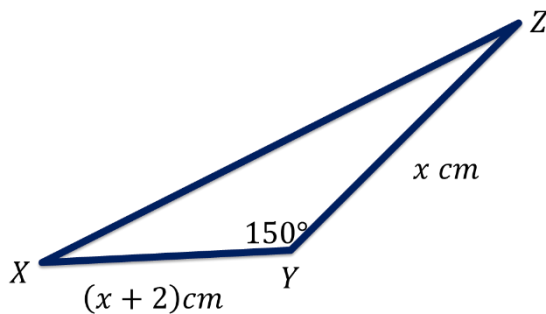
$$H = \sin^{-1}\left(4 \frac{\sin 44}{3}\right)$$

$$H = 67.851702^\circ$$

or,  $H = 180^\circ - 67.85^\circ = 112^\circ$

**Q9**

Given that the area of this triangle is  $6 \text{ cm}^2$  find the value of  $x$



$$\text{Area} = \frac{1}{2}xz \sin Y$$

$$6 = \frac{1}{2}x(x + 2) \sin 150^\circ$$

$$12 = x(x + 2) \sin 30^\circ$$

$$12 = x(x + 2) \frac{1}{2}$$

$$24 = x(x + 2)$$

$$x^2 + 2x - 24 = 0$$

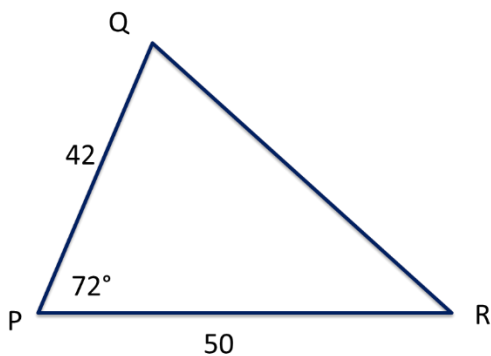
$$(x + 6)(x - 4) = 0$$

$$x = -6 \text{ or } x = 4$$

Can't have a negative length,  
therefore  $x = 4$  cm

### Q10

A builder ropes off a triangular plot of ground,  $PQR$ . The length of  $|PQ| = 42$  m and the length of  $|PR| = 50$  m.  $|\angle QPR| = 72^\circ$ . Calculate the length of rope needed by the builder. Give your answer correct to one decimal place.



Use the Cosine Rule

Pair? No      SAS? Yes =  $rPq$       Looking for  $p$

$$p^2 = r^2 + q^2 - 2rq \cos P$$

$$p^2 = 42^2 + 50^2 - 2(42)(50) \cos 72$$

$$p^2 = 1764 + 2500 - (4200)(0.30901699) = 2966.1286236$$

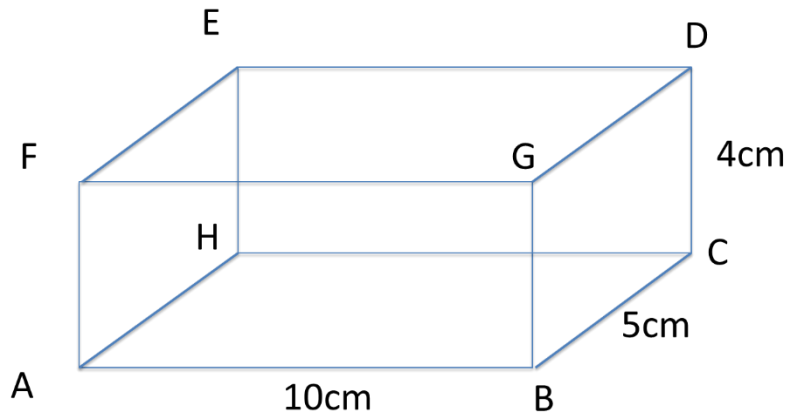
$$p = 54.4621760 = 54.5 \text{ m correct to 1.d.p.}$$

$$\text{Rope needed} = 42 + 50 + 54.5 = 146.5 \text{ m}$$

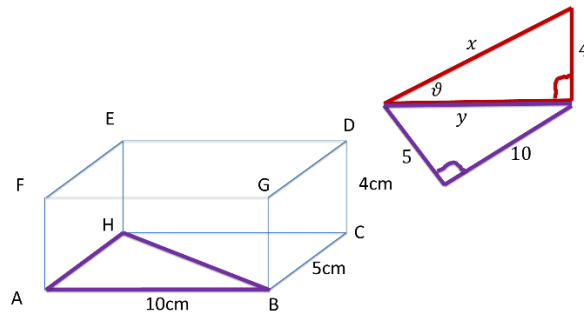
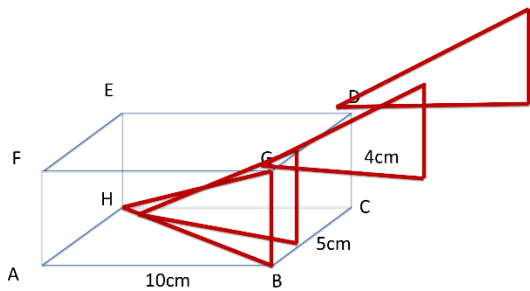


**Q11**

An open rectangular box has dimensions 10cm by 5cm by 4cm, as shown.



- 1) Find the length of the diagonal [GH].
- 2) Find the measure of the angle between GH and the base of the box.



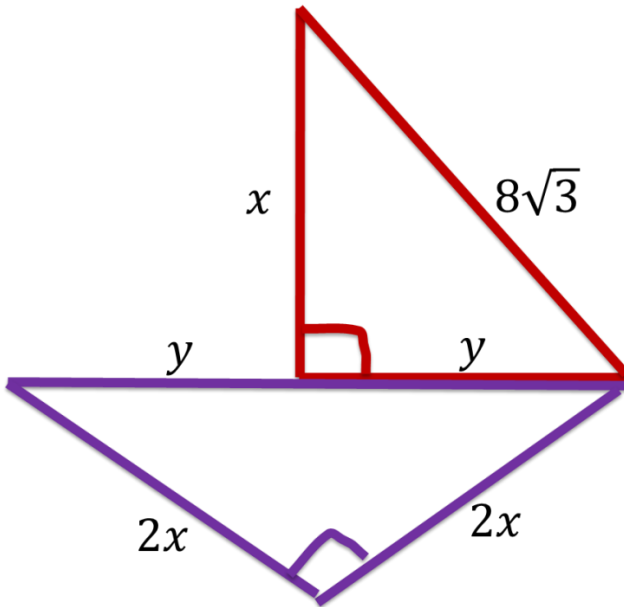
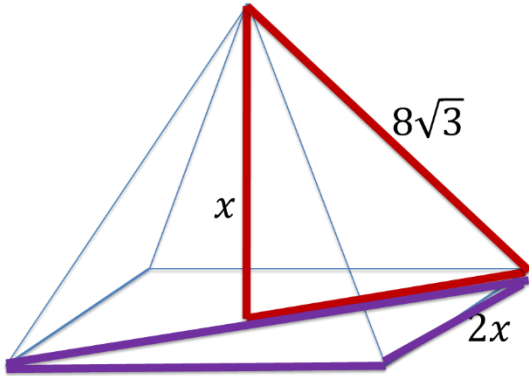
1) Use Pythagoras to find  $y = \sqrt{125}$

2) Use Pythagoras to find  $x = \sqrt{141} = 11.87434\text{cm}$

3) Use any ratio to find  $\theta$   
 eg  $\theta = \text{Tan}^{-1}\left(\frac{4}{\sqrt{125}}\right) = 19.6857^\circ$

**Q12**

The diagram represents a right pyramid. The base is a square of side  $2x$  cm. The length of each of the slant edges is  $8\sqrt{3}$  cm. The height of the pyramid is  $x$  cm. Calculate the value of  $x$ .



$$(2y)^2 = (2x)^2 + (2x^2)$$

$$y^2 = 2x^2$$

$$x^2 + y^2 = (8\sqrt{3})^2$$

$$x^2 + 2x^2 = 64 \times 3$$

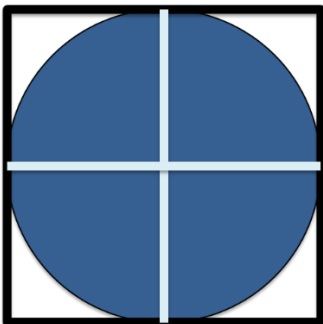
$$3x^2 = 64 \times 3$$

$$x^2 = 64$$

$$x = 8 \text{ cm}$$

**Q13**

A square is inscribed in a circle, as shown. If the area of the circle is  $\pi$  square units, find the area of the square.



$$A_c = \pi r^2 = \pi$$

$$\Rightarrow r = 1$$

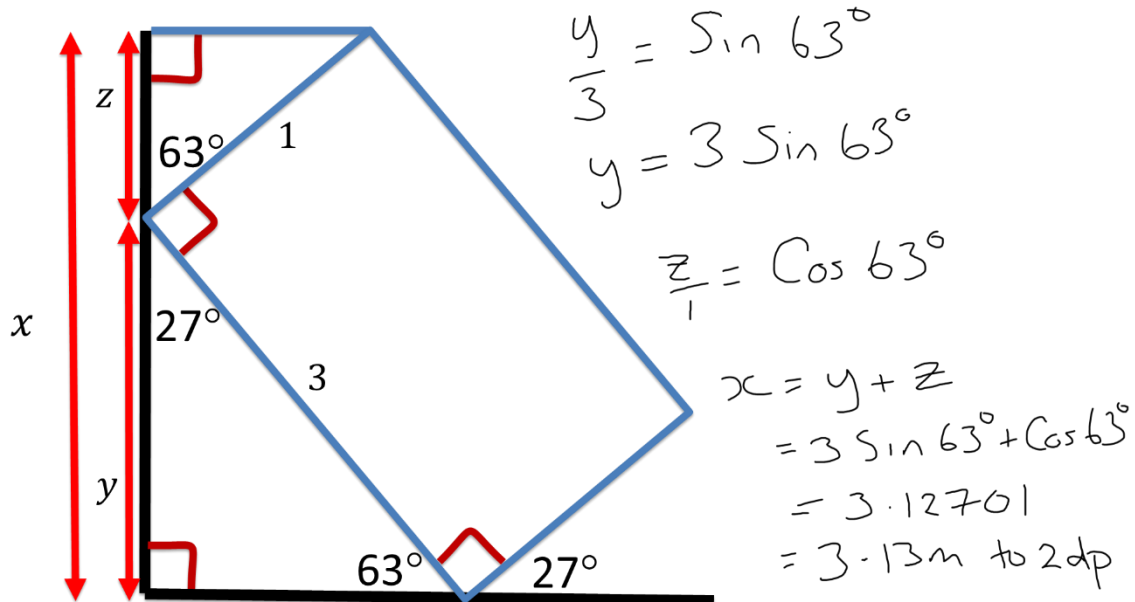
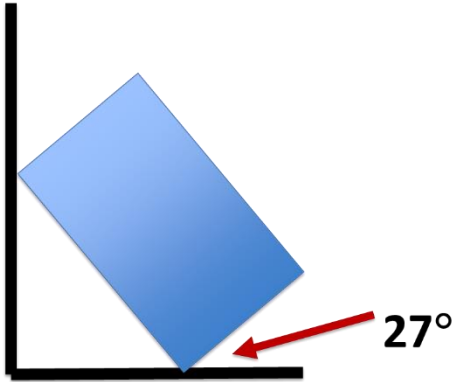
$$A_s = 2r \times 2r$$

$$= 4r^2$$

$$= 4 \text{ sq units}$$

**Q14**

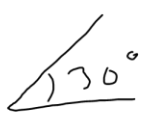
A rectangular paving stone 3m by 1m rests against a vertical wall as shown. What is the height of the highest point of the stone above the ground? Give your answer in meters, correct to two decimal places.

**Q15**

Find all the solutions to the equation  $\cos 3x = \frac{\sqrt{3}}{2}$ , for  $0^\circ \leq x \leq 360^\circ$ .

$\cos 30^\circ = \frac{\sqrt{3}}{2}$  from tables

Positive Cos in 1st and 4th quadrants



Two angles are  $30^\circ$  and  $330^\circ$

$$\text{So } 3x = 30^\circ \quad \text{or} \quad 3x = 330^\circ$$

$$x = 10^\circ \quad \quad \quad x = 110^\circ$$

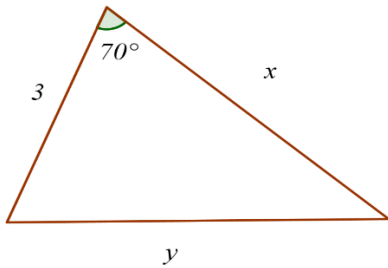
$$\text{Period} = 360/3 = 120$$

$$\text{So, } x=10+120=130, x=130+120=250, x=110+120=230, x=230+120=350$$

### Q16

The area of the triangle shown is 15 square units.

- Find the value of  $x$ , correct to two decimal places.
- Using the Cosine Rule, find the value of  $y$ .



$$\text{Area} = \frac{1}{2}zx\sin Y = \frac{1}{2}(3)(x)\sin(70) = 1.409538931179x$$

$$\text{Area} = 15 = 1.409538931179x$$

$$x = \frac{15}{1.409538931179} = 10.64178 \approx 10.64 \text{ units}$$

$$y^2 = x^2 + z^2 - 2xz\cos Y$$

$$y^2 = x^2 + 3^2 - 2x(3)\cos 70$$

$$y^2 = \left(\frac{15}{1.409538931179}\right)^2 + 3^2 - 2\left(\frac{15}{1.409538931179}\right)(3)\cos 70$$

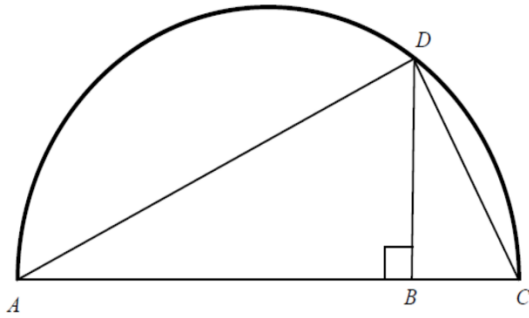
$$y^2 = 113.2474331 + 9 - 21.83821406$$

$$y^2 = 100.4092191$$

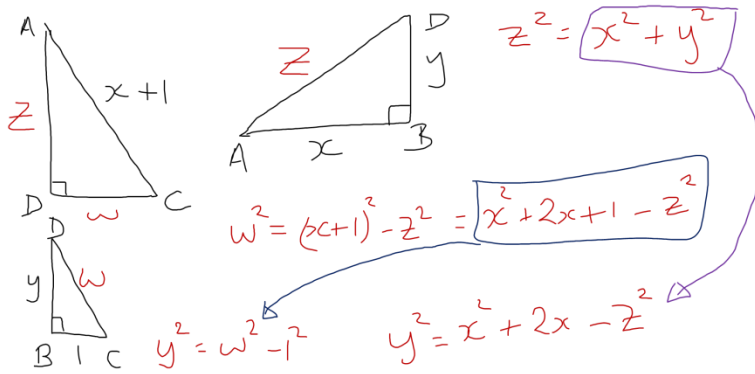
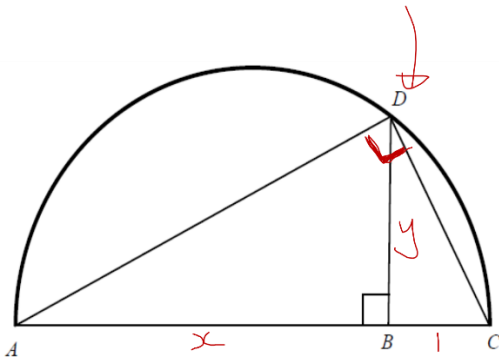
$$y = \sqrt{100.4092191} = 10.02044006 \approx 10.02$$

### Q17

The diagram shows a semi-circle standing on a diameter  $[AC]$ , and  $[BD] \perp [AC]$ .  
 If  $|AB|=x$  and  $|BC|=1$  and  $|BD|=y$ , write  $y$  in terms of  $x$ .



semi circle



$$z^2 = x^2 + y^2$$

$$y^2 = x^2 + 2x - z^2$$

$$y^2 = x^2 + 2x - (x^2 + y^2)$$

$$y^2 = x^2 + 2x - x^2 - y^2$$

$$2y^2 = 2x \quad y = \sqrt{x}$$